Postseismic deformation following the 1906 San Francisco earthquake

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Abstract. We have reevaluated triangulation data from northern California following the 1906 San Francisco earthquake, thereby increasing the temporal and spatial resolution of postseismic deformation following that event. We have calculated uniform shear strain rates and average station velocities at Point Arena using data from 1906-1907, 1929-1930, and 1973-1975 and for the Point Reyes-Petaluma arc using data from 1929-1930, 1938-1939, and 1960-1961. With the addition of recent geodetic data we infer an effective relaxation time for long-term, postseismic deformation following the 1906 earthquake of 36 ± 16 years. The Point Arena data are satisfactorily fit with accelerated afterslip at depth along the San Andreas fault plane. For a 10-km-deep, 25-km-wide afterslip zone the average slip rate between 1906 and 1930 is 11.2 cm/yr. Between 1929 and 1975 it is 4.6 cm/yr. Deformation in the Point Reyes-Petaluma arc is clearly asymmetric with respect to the trace of the San Andreas fault, especially between 1929 and 1939. After inverting for the range of acceptable accelerated deep afterslip and horizontal detachment models, a detailed analysis using geologically reasonable geometries revealed that both model types have trouble explaining the spatial variations in the deformation field through time. In particular, accelerated deep afterslip models cannot reproduce the breadths of the observed deformation field to the northeast of the San Andreas fault. As a result, more complex, time-varying deformation mechanisms are required to explain the Point Reyes-Petaluma arc observations.

1. Introduction

A great earthquake instantaneously disturbs the existing stress balance within the crust and upper mantle. Knowledge of how the resultant stress concentrations are relaxed, both temporally and spatially, can provide information about the deformation mechanisms that drive the earthquake cycle, as well as insight into the structure and rheology of the Earth's crust. Despite this, data on postseismic transients after great strike-slip earthquakes are extremely limited. The temporal resolution, duration, and spatial extent of postseismic data sets are most important for elucidating aspects of earthquake processes that occur over different timescales and length scales. In the first days to months after the 1992 $M_w = 7.3$ Landers, California earthquake, Wyatt et al. [1994] and Shen et al. [1994] measured transient deformations that were explained by postseismic aterlsip on the rupture plane and its downdip extension. Postseismic transients with durations of a few months to years are seen by Peltzer et al. [1996, 1998] and Savage and Swarc [1997] using synthetic aperture radar and Global Positioning System (GPS) data. Both Peltzer et al. [1996] and Bosl [1999] suggest that this deformation can be explained by pore pressure reequilibration. Peltzer et al. [1998] show that the multiyear record of post-Landers deformation can be explained by a combination of pore pressure reequilibration and aterlsip along portions of the coseismic rupture. Data from the 1989 $M = 7.1$ Loma Prieta, California, earthquake provide another good example [Savage et al., 1994; Burgmann et al., 1997]. Burgmann et al. [1997] conclude that short-term postseismic velocity variations can be explained by shallow aterlsip on the Loma Prieta fault plane and triggered slip on neighboring thrust faults. This is confirmed by Pollitz et al. [1998] who find that to this point, only a small portion of the post-Loma Prieta deformation can be attributed to deep asthenospheric sources. Similar results are seen after the 1994 $M = 6.7$ Northridge, California, event [Donnellan and Lyzenga, 1998]. These studies focus on postseismic transients generated by shallow sources that decay rapidly with time after an event.

Geodetic data spanning the first decades after an event are more likely to provide information about long-period relaxation of structures in the lower crust and upper mantle. The problem is that postseismic data of this temporal extent are generally unavailable, particularly in strike-slip regimes such as California, because of the relatively recent advent of sufficiently accurate geodetic measurements. Also, significant postseismic relaxation of the lower crust and asthenosphere may only be triggered by great strike-slip events. Asthenospheric relaxation has been suggested as an explanation for long-duration, ≥ 5 year, transients [Savage and Swarc, 1997] after the 1992 Landers event [Pollitz et al., 2000, Deng et al., 1998]. Data after the largest events on the San Andreas fault system are limited to triangulation measurements following the 1906 $M = 8.3$ San Francisco [e.g., Thatcher, 1973a, b] and 1857 $M = 8$ Fort Tejon earthquakes [Pollitz and Sacks, 1992].

To date, only uniform shear strain rate estimates are available following the 1906 event (Figure 1). Thatcher [1975b], Cline et al. [1985], and Gilbert et al. [1993] used available geodetic data from the northern California primary arc (Figure 1) to calculate uniform strain rates for various geographic regions, but each region encompasses hundreds of
square kilometers and the uniform strain assumption may not be valid. Thatcher [1975a, b] calculated uniform shear strain rates for a number of small aperture networks in northern California, but used only repeated angle measurements. At Point Arena, Thatcher [1975a], Thatcher et al. [1997], and Matthews and Segall [1993] used triangulation data from 1891 to 1906-1907 to estimate the magnitude and depth of coseismic slip during the 1906 earthquake. Thatcher's [1975a] results give 5.0 ± 0.05 m of slip to 10 km depth. Matthews and Segall [1993] allow for variable slip at depth and estimate a 15-20 km depth of faulting with ~6 m of slip at the surface.

Postseismic studies have computed only total deformation rates following the 1906 San Francisco earthquake. Thatcher [1975a] finds that triangulation data between 1906 and 1930 at Point Arena can be satisfactorily explained by ~3.1 ± 0.5 m of slip between 10 and 30 km depth, a slip rate of ~0.13 m/yr. Thatcher [1975b] and Cline et al. [1985] investigated the post-1906 distribution of shear strain within the Point Reyes-Petaluma arc. Both studies show a nonuniform distribution of deformation with accelerated strain rates at the trace of the Rogers Creek fault. In both cases, anomalous strain rates seen southwest of the San Andreas fault were largely attributed to observational errors. Regardless, both Thatcher [1975b] and Cline et al. [1985] see decreasing deformation rates when comparing the 1930-1938 and 1938-1961 observation intervals. Finally, Thatcher [1983] compiled uniform strain rate estimates from both northern and southern California to infer an ~30 year relaxation time for long-term postseismic deformation within the San Andreas system. The use of strain rates from both northern and southern California could be questioned, however, because, as noted by Thatcher [1983], the tectonic regime may be different along the 1906 and 1857 segments of the fault.

In this study, we improve upon prior post-1906 analyses using the methods of Yu and Segall [1996], which allow all triangulation measurements, not just repeated angles, to be analyzed. This allows us to include previously unanalyzed triangulation data, especially at Point Arena. With the addition of more recent geodetic data, we are able to determine strain rates at multiple times and infer a relaxation time for long period postseismic deformation along geographically limited segments of the San Andreas fault. We also invert for the distribution of postseismic slip at depth as a function of time. In addition to deep afterslip models we test the applicability of detachment models [e.g., Furlong et al., 1989]. Finally, for each network, we have for the first time been able to estimate station velocities, allowing for a more
detailed investigation of both the spatial and temporal distribution of postseismic deformation after the 1906 earthquake. Information of this type will prove instrumental in discriminating between competing hypotheses regarding deformation mechanisms in northern California [e.g., Kenner and Segall, 1999a].

2. Data

Available triangulation data were obtained from the National Geodetic Survey (NGS). The angles between stations were determined from the observed direction lists. For each network or subnetwork, improved station coordinates were then estimated using the triangulation data from all epochs, i.e., ignoring any deformation that might have occurred [Yu and Segall, 1996]. If the normalized angle residual to the station adjustment was greater than five standard deviations, it was removed from all stages of the analysis. In general, the direction measurements that were eliminated ended up being suspected blunders, as recorded in the NGS datafiles. Subsequently, observations suspected to be blunders by NGS were removed only if the normalized residual exceeded the largest normalized residual that had not been flagged as a suspected blunder. Though it does not change the qualitative inferences of the work, the quantitative results are somewhat dependent on the details of this procedure.

We concentrated our efforts on two networks, the Point Arena net and the Point Reyes-Petaluma are. Triangulation surveys (Figure 2) in the vicinity of Point Arena were completed in 1906-1907, 1925, 1929-1930, and 1973-1975. Between 1991 and 1995 a substantial portion of the 1906-1907 network was reoccupied using GPS [Freymueller et al., 1999]. Since stations surveyed in 1925 lie primarily to the northeast of the San Andreas fault and stations surveyed in 1929-1930 lie primarily to the southwest, we chose to analyze the 1906-1907, 1925, and 1929-1930 data sets simultaneously. Though this approach neglects differences in

Figure 2. Point Arena surveys of 1906-1907, 1925, 1929-1930, and 1973-1975. The majority of the 1906-1907 network was resurveyed using GPS between 1991 and 1995.
the deformation rate during the two time intervals, we feel that the improved spatial resolution compensates for the very minor improvements in temporal resolution that are obtained by analyzing the 1906-1907 to 1925 and 1925 to 1929-1930 data separately. Next, we analyzed the 1929-1930 and 1973-1975 data sets. Given limited network overlap and large uncertainties, a comparison of 1925 and 1973-1975 triangulation data was not warranted. GPS velocities between 1991 and 1995 were taken, without modification, from Freymueller et al. [1999]. Though the GPS survey extended much farther to the northeast, we use only those stations that lie within the aperture of the 1906-1907 triangulation network for our calculations.

The Point Reyes Petaluma arc (Figure 3) extends from Point Reyes Head, ~20 km to the southwest of the San Andreas fault, to the vicinity of Petaluma, ~45 km to the northeast. This entire profile was surveyed in 1929-1930, 1938-1939, and 1960-1961. Subsequent surveys of the region were completed in the 1970s, 1980s, and 1990s using trilateration and/or GPS [Prescott and Yu, 1986; Lisowski et al., 1991; Lisowski and Savage, 1992; Williams et al., 1994; Williams, 1995; Murray et al., 1998; Savage et al., 1999]. We use the results of Lisowski and Savage [1992] to complement the historical triangulation data at this location. GPS velocities between 1993 and 1998 [Murray et al., 1998; Savage et al., 1999] are nearly indistinguishable from those of Lisowski and Savage [1992], but the station density near the San Andreas fault does not allow for the calculation of shear strain rates in small fault-crossing networks, as required for direct comparison with the triangulation data.

Parts of the northern California primary network were surveyed in 1906-1907, 1922-1923, 1925, 1929-1930, and 1948 (Figure 1). The total aperture of the network is >120 km. It includes the Farallon Islands, located ~40 km southwest of the San Andreas fault. Estimates of station velocities in a network of this spatial and temporal extent would allow greater resolution of the distribution of post-1906 deformation, particularly to the southwest of the San...
Andreas fault. Unfortunately, though we were able to reproduce the uniform strain values of Thatcher [1975a], reasonable velocity estimates for the primary network were not obtained. While typical baselines in the Point Reyes- Petaluma and Point Arena networks average under 10 km, baselines in the primary network are tens of kilometers in length with some extending to 90 km. As a result, the uncertainties in the velocity determinations are unacceptably large. Additionally, many of the baselines run along the coastline and may be subjected to large refraction errors resulting from unmodeled gradients in the index of refraction [see Bomford, 1980, Sections 1.36-1.37].

3. Analysis

3.1 Uniform Shear Strain Rates

Uniform shear strain rates were calculated from the triangulation data using the approach of Yu and Segall [1996]. Uniform shear strain rates associated with the modern geodetic data were calculated from the published station velocities. The best fitting exponential decay rate for the fault parallel shear strain rate was then determined using a least squares solution to a linear reparameterization of the strain rate data in semilog space. This provides an estimate of the average effective exponential relaxation time for time-dependent deformation in the crust and upper mantle following the 1906 San Francisco earthquake. The relaxation time is defined as twice the effective viscosity divided by the shear modulus. The approach presumes that the data in the original parameterization are non-Gaussian [Menke, 1989, p. 147]. Though this is not necessarily the case, given the limited number of data, we felt that a more complicated approach was not warranted. In addition, inversions for the best fitting model in semilog space account for the fact that the strain rates represent averages over multiyear time intervals. Since the inversion is linear in this case, the average \( \ln(\text{strain rate}) \) during any time interval is equivalent to the \( \ln(\text{strain rate}) \) at the median or representative time of that interval. An exponential fit is used because this is the form of the first term in the analytical series solution for surface strain rate in an elastic plate overlying a viscoelastic half-space [Nur and Mavko, 1974; Savage and Prescott, 1978]. It has been shown that a model of this type can satisfactorily approximate the postseismic response of the San Andreas fault system after great events [Thatcher, 1983].

At Point Arena, uniform shear strain rates between 1906-1930, 1929-1975, and 1991-1995 yield a best fitting exponential relaxation time of 29 ± 15 years. Uniform shear strain rates for a subset of the Point Reyes-Petaluma arc, the Point Reyes network (Figure 3, inset) of Thatcher [1975a, 1983], for the time periods 1929-1939, 1938-1961, and 1973-1990 are also determined. Using these shear strain rates, the best fitting exponential relaxation time for postseismic deformation at Point Reyes is estimated to be 79 ± 30 years, but data immediately following the 1906 earthquake, when the rates of change are highest, are unavailable. Combining the Point Arena and Point Reyes data yields a 36 ± 16 years estimate of the relaxation time in northern California (Figure 4). If the average shear modulus of the relaxing materials is assumed to be 6x10^8 MPa [Thatcher, 1983], this corresponds to an effective viscosity of \( \sim 3.4x10^{19} \) Pas.

Additional subnetworks of the Point Reyes-Petaluma arc (Figure 5) were used to investigate the spatial distribution of shear strain for the time periods 1929-1939 and 1938-1961 using the Yu and Segall [1996] methodology (Figure 5). During the 1929-1939 time interval, relatively high maximum shear strain rates are broadly distributed between the San Andreas and Rogers Creek faults. Shear strain rates between 1938 and 1961 are generally smaller than those between 1929 and 1939. The only exception are the two subnetworks that include the Rogers Creek fault and areas to the northeast. In both time periods the shear strain rate profile is asymmetric with respect to the trace of the San Andreas fault. Estimated directions of maximum right-lateral shear are more consistent with the strike of the San Andreas fault during the second time interval than during the first.

These same networks and subnetworks were used by Thatcher [1975a, b] and Cline et al. [1985]. Though the solutions are based on the same data, in some instances they differ at the 1σ level. At Point Arena our results agree with those of Thatcher [1975a, 1983]. For the Point Reyes-Petaluma arc our solution has fewer outliers and seems to vary more smoothly with distance from the San Andreas fault than the results of Thatcher [1975b] and Cline et al. [1985]. This may reflect use of a more robust method for dealing with historical triangulation data. We include more angle measurements than Thatcher [1975b], while Cline et al. [1985] calculate strains from least squares determined displacements. Cline et al. [1985] also include long baselines extending to Fort Ross and Mount Tamalpais. While inclusion of these baselines is beneficial when estimating displacements in long narrow networks, such as the entire Point Reyes-Petaluma arc, inversions for strain using small networks yields higher spatial resolution. As a consequence, we prefer to calculate uniform shear strain rates directly from the data using only those stations within each subnetwork.

![Figure 4](image-url). Evolution of uniform shear strain rate with time since the 1906 San Francisco earthquake at Point Arena (circles) and Point Reyes (triangles). Vertical error bars give 1σ uncertainties. Horizontal error bars give the time between the first and last surveys included in the inversion. The solid line is the best fitting exponential regression to the data. Strains have been rotated 20° (clockwise) and 10° (clockwise), respectively, from north so that \( \gamma \) represents the right-lateral shear strain rate across that San Andreas fault.
The variations among the different solutions may also reflect differences in how suspected blunders were treated.

3.2 Inversions for Slip at Depth

Assuming post-1906 deformation can be adequately represented by afterslip at depth, we attempt to infer the distribution of slip as a function of time on either the down-dip extension of the 1906 rupture or a detachment lying northeast of the San Andreas fault. Specifically, for each time interval being considered, we use an elastic dislocation model to invert for acceptable distributions of slip at depth. Unfortunately, the triangulation networks are not broadly distributed about the San Andreas fault, severely limiting depth resolution. The limited resolution forced us to divide the San Andreas fault into only three depth intervals. The shallowest interval represents a zone of accelerated postseismic afterslip. The third interval extends to infinite depth and represents deep slip at a constant rate of 70 mm/yr [Kelson et al., 1992; Freymueller et al., 1999]. Free parameters in the accelerated afterslip model are the depth to the top and width of the afterslip zone and the rate of fault slip. Detachment model parameters are depth, fault-perpendicular width of the detachment surface, and slip rate. The southwestern edge of the detachment surface is assumed to be colocated with the trace of the San Andreas fault. To test the hypothesis that the deep plate boundary is located northeast of the San Andreas fault, no slip is allowed below the detachment surface along the San Andreas fault. Also, the Hayward-Rogers Creek-Maacama fault is assumed to slip at 50 mm/yr below the level of the detachment surface. This is approximately equal to the combined San Andreas and Hayward-Rogers Creek-Maacama fault slip rates [Bürgmann et al., 1994, 1997]. Shallow creep,
in accordance with the secular model, is also allowed. As models incorporating a viscoelastic lower crustal channel or asthenosphere [Thatcher, 1983; Li and Rice, 1987; Savage, 1990] would likely be indistinguishable from the deep afterslip model on the basis of this dataset [Savage, 1990], they are not explicitly addressed.

In each inversion, the secular model of Bürgmann et al. [1994, 1997] is used to model slip on all faults other than the portion of the San Andreas and/or Hayward-Rogers Creek-Macama faults being considered. The secular model extends from approximately the latitude of Parkfield, California, north to Point Arena. For our purposes the three subparallel faults in northern California were extended from Point Arena to Cape Mendocino. They were modeled as single fault segments slipping below ~10 km depth.

The slip model minimizing the weighted residual sum of squares was found using a simple grid search. A linear least squares solution was used to specify the optimal slip rate for each set of geometric parameters (depth and width). Confidence intervals were derived using an F test [e.g., Arnadóttir and Segall, 1994]. In spite of the fact that this approach underestimates actual confidence limits [Arnadóttir and Segall, 1994], our results indicate the data place only weak constraints on the depth extent of afterslip. This is not surprising given the spatial extent of the networks. Additional constraints can be applied if we assume that the 1906 San Francisco earthquake was a characteristic event and neglect plastic deformation in the crust adjacent to the fault (i.e., we assume that at long timescales the lithospheric plates move as rigid bodies). Using these assumptions, we can state that

\[
\int_{T_{cycle}} \dot{s}(t) dt = S,
\]

where \( \dot{s} \) is the slip rate at any depth, \( S \) is the characteristic earthquake slip, and \( T_{cycle} \) is the characteristic earthquake cycle time. If (1) is discretized into finite temporal epochs, we have

\[
\sum_{j=1}^{n} \dot{s}_j (t_{j+1} - t_j) = S,
\]

where \( \dot{s} \) is the average slip rate during time interval \( (t_{j+1} - t_j) \). Using (2), we can then bound the slip rate during any particular time interval by assuming that \( S \) provides an upper bound on the amount of slip that can take place in any depth interval during one complete earthquake cycle:

\[
\dot{s}_j \leq \frac{S}{(t_{j+1} - t_j)},
\]

If we have estimates of the slip during one or more prior intervals, then at any depth we can use (2) to generate more detailed constraints of the form

\[
S = \sum_{j \text{ Prior Estimates}} \dot{s}_j (t_{j+1} - t_j)
\]

Given the limited depth resolution of the data, we assume that the depth extent of the accelerated afterslip zone does not change with time. Especially at Point Arena, we find slip rate constraints of this type, based on the expected characteristic slip, to be more restrictive than the formal confidence intervals. Estimates of the amount of coseismic slip during the 1906 San Francisco earthquake range from ~5 to 7 m [Thatcher, 1975a; Thatcher et al., 1997, Matthews and Segall, 1993]. All results are summarized in Table 1. Because uncertainties in the model inversions are large, only model bounds, as defined by the slip rate constraint and the 95% confidence interval, are listed.

Optimal slip rates for a deep afterslip model of deformation between 1906-1930 and 1929-1975 at Point Arena are shown in Plates 1a and 1b. For both time intervals the data constrain the top of the zone of postsismic slip to be no shallower than 1-2 km. Owing to the narrow aperture of the network, the width of the zone of accelerated afterslip is unconstrained. Between 1906 and 1930 the 95% confidence level and a slip rate constraint (equation (3)) requires that the top of the postsismic afterslip zone be no deeper than 20 km. Allowable slip rates are between ~2 and 24 cm/yr. During the 1929-1975 time interval a slip rate constraint that includes prior slip between 1906 and 1930 (equation (4)) requires the top of the postsismic afterslip zone be no deeper than 12.5 km. For each set of geometric parameters the appropriate 1906-1930 slip rate is used in the constraint calculation. Allowable 1929-1975 slip rates are between ~0 and 5.8 cm/yr. If the accelerated afterslip zone is constrained to be 25 km wide with a top depth of 10 km, consistent with 1) the slip rate constraint during both time intervals, 2) the maximum depth of seismicity in California, and 3) Thatcher's [1975a] estimate of the depth of coseismic faulting during the 1906 earthquake, the slip rate evolves with time as shown in Figure 6.

Inversion results for the best fitting accelerated afterslip zone during the 1929-1930 time interval at Point Reyes-Petaluma are shown in Plate 1c. At 95% confidence the top of the afterslip zone must be above 21.5 km depth, while the width is entirely unconstrained. Slip rates range between ~0 and 53 cm/yr. The slip rate constraint (equation (3)) is less

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* Width is required to be at least 2 km in the inversion. Maximum widths are not well constrained by the inversion for most parameter combinations.
Plate 1. Optimal slip rate as a function of the top depth and width of the zone of accelerated aterlsip for the deep afterslip model at the Point Arena network between (a) 1906 and 1930 and (b) 1929 and 1975 and for the Point Reyes-Petaluma arc between (c) 1929 and 1939 and (d) 1938 and 1961. Optimal models, shown by the red asterisk, give Plate 1a) a slip rate of 62 mm/yr between 6 and 42 km (misfit of 1.053), Plate 1b) a slip rate of 16 mm/yr between 4 and 54 km (misfit of 1.035), Plate 1c) a slip rate of 10 mm/yr between 2 and 24 km (misfit of 1.389), and Plate 1d) a slip rate of 2 mm/yr between 1 and 11 km (misfit of 1.243). Black lines with white dashes denote 50%, 90%, and 95% confidence levels. White areas are not allowed at 95% confidence. Gray areas are excluded using the characteristic slip constraint that allows 5.5 m of coseismic slip at Point Arena and 6.5 m at the Point Reyes-Petaluma arc. In Plates 1a and 1c the slip constraint is derived using equation (3). In Plates 1b and 1d the slip constraint is derived using equation (4) and slip rates from the 1906-1930 Point Arena inversion and 1929-1939 Point Reyes-Petaluma inversion, respectively.
of coseismic faulting in 1906 [Thatcher, 1975a; Matthews and Segall, 1993], and the seismic reflection data [Holbrook et al., 1996].

3.3 Station Velocity Estimates

Velocity estimates were obtained from the triangulation data using a slightly altered form of the methods described by Yu and Segall [1996]. They solved for the station displacements using data from two different triangulation surveys. We generalized their method, solving for station velocities using data from an arbitrary number of surveys. As described by Yu and Segall [1996], the initial station coordinates $x_i$ are obtained using an iterated minimum norm solution to update the a priori station coordinates. Using the notation of Yu and Segall [1996], the observation equations, linearized about these coordinates [Yu and Segall, 1996, equations (6) and (7)], are

$$d\theta_n = A_n dx_n + e_n$$

where $n$ is the number of different surveys that will be included in the inversion, $A_n$ represents the network geometry at time $t_n$ with stations at coordinates $x_n$, $e_n$ are the measurement errors, and $d\theta_n - \theta_n(x) - \theta_n(x_i)$ represents the difference between the observed angles and those estimated from the initial station coordinates, $x_i$, at time $t_i$, the time of the earliest survey. The change in position for all subsequent surveys can then be defined as

$$d\Delta x_n = d\Delta x_1 + v dt_n,$$

where $v$ are the station velocities, $dt_n = t_n - t_1$, and $t_n$ is the date of survey $n$. If a survey took place over multiple years, it was assigned a date representative of the midpoint of its duration; for example, the 1929–1930 survey was assigned a date of 1929.5. The full system of equations can now be written as

$$
\begin{bmatrix}
  d\theta_1 \\
  d\theta_2 \\
  \vdots \\
  d\theta_n
\end{bmatrix}
= 

\begin{bmatrix}
  \mathbf{A}_1 & 0 & 0 & \cdots & 0 \\
  \mathbf{A}_2 & \mathbf{A}_2 dx_1 & 0 & \cdots & 0 \\
  \vdots & \vdots & \vdots & \ddots & \vdots \\
  \mathbf{A}_n & \mathbf{A}_n dx_n & \mathbf{A}_n & \cdots & \mathbf{A}_n
\end{bmatrix}
\begin{bmatrix}
  \mathbf{v}_1 \\
  \mathbf{v}_2 \\
  \vdots \\
  \mathbf{v}_n
\end{bmatrix},
$$

which for compactness can be rewritten as

$$d\Delta \theta = \Psi d\mathbf{x} + \Omega v + \varepsilon, \quad \varepsilon \sim N(0, \Sigma),$$

where

$$
\Sigma = \begin{bmatrix}
  \Sigma_1 & 0 & 0 & 0 \\
  0 & \Sigma_2 & 0 & 0 \\
  0 & 0 & \ddots & 0 \\
  0 & 0 & 0 & \Sigma_n
\end{bmatrix}
$$

and $\Sigma_i$ are the data covariances for each survey. Equations (8) and (9) are equivalent to equations (10) and (11) of Yu and Segall [1996]. The station velocities are then determined using exactly the same procedure that Yu and Segall [1996] used for determining station displacements, except that $\mathbf{u}$ is replaced by $\mathbf{v}$ in all subsequent equations. As before, corrections to the station coordinates are removed from the governing equations by premultiplying (8) by $(\mathbf{I} - \Psi \Psi^T)$ where $\Psi^T$ is the generalized inverse of $\Psi$. Since triangulation data do not constrain rigid body rotations, translations, or dilatation, we present model coordinate velocities [Segall and
Figure 7. Total (a) fault-parallel (N25°W) and (b) fault-normal model coordinate velocities, with 1σ uncertainties, as a function of distance from the San Andreas fault at Point Arena. Model coordinate velocities are estimated using a 25-km-wide afterslip zone whose top is located at 10 km depth. The slip rates are 11.2 cm/yr and 4.6 cm/yr for the 1906-1930 and 1929-1975 periods, respectively (Figure 6). Velocities are plotted relative to the velocity at station Lnc. Model predictions are given by the appropriate lines. The model for the 1991-1995 GPS velocities is taken from the inversion results, using data from all of northern California, of Preymueller et al. [1999] for the San Andreas fault that give 17.4 mm/yr of slip below 14.9 km depth.

Matthews, 1988]. Solutions of this type depend on a prior model to provide a reference frame for the solution and constrain the null space, those components of the solution that are not constrained by the data. In practice, since network rotations and strike-slip deformation look the same in narrow fault-perpendicular networks, use of model coordinate velocities means that increasing the amount of slip at depth on the San Andreas fault in the prior model increases the resultant velocities in an antisymmetric sense about the San Andreas fault. This effect is most pronounced in the Point Arena network. Because the Point Reyes-Petaluma arc is braced by stations at Mount Tamalpais, Ross Mountain, and Mount Helena, the effect is significantly reduced.

The model coordinate station velocity estimates at Point Arena are derived using the best fitting model with afterslip between 10 and 35 km depth (Figure 7). Secular slip rates are applied to all other faults and depth intervals. As shown, the computed velocities on either side of the fault clearly decrease and become smoother with time. Further, they are consistent with the prior model. While this does not mean that the model is correct, it does mean that it is consistent with the spatial distribution of deformation. When only the secular model of Bürgmann et al. [1994, 1997] is used to constrain the null space, the trends in the resultant velocities, which represent a probable minimum bound on fault-parallel velocity magnitudes, are still discernible, though the prior model is clearly inconsistent with the 1906-1930 data.

The Point Reyes-Petaluma arc velocities as determined using the best fitting model with afterslip between 10 and 35 km depth are given in Figure 8. During the 1929-1939 time interval the prior model is inconsistent with the data. It is more appropriate during the 1938-1961 interval, though the fault parallel velocities are still slightly underpredicted. Regardless, it is apparent that velocities to the northeast of the San Andreas fault decrease with time following the 1986 San Francisco earthquake. This variation in velocity with time remains even when a purely secular prior model is used to constrain the null space. The trends in the velocity distribution through time to the southwest of the fault are more problematic. The 1929-1939 velocities show little shear strain accumulation and possess a component of fault normal contraction within ~20 km of the San Andreas fault. Shear strain rates for the same region (Figure 5a) are highly uncertain with directions of maximum right-lateral shear strain which are inconsistent with the regional deformation field. This anomalous deformation was previously attributed to observational errors by Thatcher [1975b] and Cline et al. [1985]. Geometric inconsistencies in the network at this location probably contribute as well. In spite of this, the 1929-1939 results clearly indicate important postseismic spatial variations and asymmetries in the deformation field at the latitude of Point Reyes.

4. Discussion

As mentioned, the quantitative results are, to a certain extent, a function of how suspected blunders were dealt with during initial processing of the triangulation data. Changes
are only significant for the slip inversions and velocity estimates involving data from the entire Point Reyes-Petaluma arc in 1929-1930. Other networks, subnetworks, and time intervals contain fewer suspected blunders so that the solutions are less sensitive to the treatment of outliers. In the extreme, if all suspected blunders and data of questionable reliability from the southwest of the San Andreas are removed from the 1929-1930 Point Reyes-Petaluma data set, inversions for slip at depth are far less constrained and the inferred slip rates are lower for any given geometry. Estimated model coordinate velocities to the northeast of the San Andreas fault between 1929 and 1939 are also lower, though they are still slightly higher than during the 1938-1961 time interval and the nearly linear trend in velocity northeast of the San Andreas fault persists. Inversions using this reduced data set have a normalized misfit that is ~8% smaller than inversions using the entire data set.

Prior analyses of postseismic deformation following the 1906 San Francisco earthquake have not been very detailed because they have been limited to estimates of uniform shear strain rate and simple dislocation models with assumed a priori constraints. With the improved methods of Yu and Segall [1996] and the addition of more recent geodetic results, we have been able to obtain much better spatial and temporal resolution of postseismic deformation following the 1906 earthquake. Estimates of the relaxation time for long-term postseismic deformation at Point Arena and Point Reyes are in agreement with estimates of ~30 years made by Thatcher [1983] for the entire San Andreas fault. This supports the conclusion that there are long-term postseismic transients, probably generated by deep sources in the lower crust and upper mantle, after great events within the San Andreas fault system.

The presence of long-term postseismic transients is also discernible in our estimates of the spatial distribution of deformation. We find that geodetically observable deformation transients following the 1906 earthquake have, within observational uncertainties, largely disappeared by about 1940. Shear strain rates within the Point Reyes-Petaluma arc generally decay with time. The primary exception is the subnetwork that crosses the Rogers Creek fault. This may be explained by the fact that the 1906 San Francisco earthquake moved both the shear stress and the Coulomb failure function on the Rogers Creek fault away from failure [Simpson and Reasenberg, 1994; Jaumé and Sykes, 1996; Kenner and Segall, 1999a]. Postseismic strain accumulation and creep rates immediately following the 1906 earthquake would therefore be expected to be lower at this location. Velocities at both the Point Arena and Point Reyes-Petaluma arcs are also higher during the earliest time intervals. During subsequent time intervals the velocities are nearly indistinguishable from the modern geodetic results.

Our deformation estimates provide snapshots of the evolution of the spatial distribution of postseismic deformation.

![Graph](image-url)

**Figure 8.** Total (a) fault-parallel (N35°W) and (b) fault-normal model coordinate velocities, with 1σ uncertainties, as a function of distance from the San Andreas fault for the Point Reyes-Petaluma arc. Model coordinate velocities are estimated using a 25-km-wide asperity zone whose top is located at 10 km depth. The slip rates are 4.0 cm/yr and 2.8 cm/yr for the 1929-1939 and 1938-1961 periods, respectively (Figure 6). Triangulation results are plotted relative to the velocity at Langdon. The 1973-1990 velocities [Lisowski and Savage, 1992] are plotted relative to the velocity at a nearby station, Seic. Model predictions are given by the appropriate lines. The 1973-1990 results are plotted with the secular model of Bürgmann et al. [1994, 1997].
deformation at Point Arena and Point Reyes through time. Recent geodetic data indicate that the velocity field [Freymueller et al., 1990; Williams et al., 1994; Lisowski et al., 1991; Prescott and Yu, 1986] is not antisymmetric about the trace of the San Andreas fault, as one would expect if the San Andreas accommodates the majority of the Pacific-North American relative plate motion. Postseismic velocities from Point Arena do not exhibit profound asymmetries with respect to the trace of the San Andreas fault, though the aperture of the network is too narrow to permit strong conclusions. In contrast, shear strain rates and velocities in the Point Reyes-Petaluma arc show pronounced asymmetry, particularly between 1929 and 1939. As a consequence, we consider geologically reasonable models of deformation within the Point Reyes-Petaluma arc in more detail. We will compare these models to the available shear strain rate estimates (Figure 9) as these are our most fundamental results. Recall that estimated velocities are model coordinate velocities and therefore depend on a prior model. The velocity estimates at each station are also highly correlated with one another. This means that visual evaluations of inconsistencies between the prior model and the data can be deceiving because the eye cannot account for the existing correlations.

The first model, a purely secular model [Burigmann et al., 1994, 1997], provides a reference for subsequent models which incorporate additional sources of postseismic deformation. The purely secular model is clearly inconsistent with the shear strain rates during the earliest time interval, 1929-1939. Observed fault parallel shear strain rates ($\gamma_1$) are underpredicted within an 20 km wide zone extending to the northeast of the San Andreas fault (Figure 9a). Fault parallel shear strain rates to the northeast of the Rogers Creek fault are overpredicted. A purely secular model is more appropriate during the 1939-1961 time interval, though fault parallel shear strain rates near the San Andreas fault are still underpredicted (Figure 9b). The second model is the best fitting model with afterslip between 10 and 35 km depth (slip rates as in Figure 6). During the 1929-1939 time interval this model does a much better job of fitting the peak fault parallel shear strain rates at the San Andreas fault, but still does not satisfactorily describe the breadth of the postseismic deformation field to the northeast. Between 1938 and 1961 the deep afterslip model is very similar to the purely secular model, though in this case fault parallel shear strain rates near the San Andreas fault are slightly overpredicted. The third model, the best fitting 15-km-deep horizontal detachment surface, satisfactorily describes both the magnitude and spatial variation in the fault parallel shear strain between 1929 and 1939. During the 1938-1961 time interval the detachment model significantly overestimates fault parallel strain rates between the San Andreas and Rogers Creek faults. Furthermore, while the presence of a horizontal detachment surface is predicted by some models of the thermomechanical evolution of the San Andreas fault system [Furlong et al., 1989], it seems to contradict recent seismic reflection work in the San Francisco bay [Parsons and Hart, 1998] and northern California [Henstock et al., 1997], which find evidence for discrete faults extending through the lower crust. None of the models fit the estimated $\gamma_1$ values very well (Figure 9). Thus these models do not seem completely satisfactory. In all cases, they fail to represent some portion of the data, and all have difficulty reproducing the time dependence of the deformation.

Other hypotheses have been put forth as an explanation for the asymmetry in the deformation field across the San Andreas fault. One involves differences in mechanical properties between oceanic and continental crust. Lisowski et al. [1991] investigated the effect of variations in material properties across the San Andreas fault in northern California using 1973-1989 trilateration data. They concluded that the required rigidity contrasts were unrealistic. Because the
asymmetry is enhanced immediately following the 1906 event, this problem would be exaggerated when attempting to describe the 1929-1939 data. A second option is the presence of a low-rigidity San Andreas fault zone. Lisowski et al. [1991] showed that existence of such a zone can effectively decouple the two sides of the fault, regardless of the contrast in material properties across it, though required rigidities within the fault zone may be too low to be realistic. Thus variations in material properties alone seem incapable of explaining the observed asymmetry.

Another possible explanation for the asymmetry is the occurrence of accelerated deep afterslip not only below the San Andreas fault but also below neighboring subparallel faults to the northeast. This would help explain the nearly constant fault parallel shear strain rates (i.e., the linear trend in fault-parallel velocity) to the northeast of the San Andreas fault. This linear trend, whose slope decreases with time, is apparent in each of the time intervals under consideration (Figure 8a). The modern velocity field can be effectively explained using a multiple fault dislocation model with deep slip beneath each of the three subparallel faults in northern California [Freymuller et al., 1999; Lisowski et al., 1991; Prescott and Yu, 1986]. It seems reasonable therefore to assume that the postseismic velocity fields could be explained in a similar fashion. The problem, as mentioned previously, is that the 1906 event moved neighboring subparallel faults away from failure. One would therefore not expect them to slip at faster rates. Fault-parallel shear strain rates in the subnetwork spanning the Rogers Creek fault are indeed lower between 1929 and 1939 as compared to the 1938-1961 time interval (Figure 5). On the other hand, if structures with low effective viscosities exist in the lower crust northeast of the San Andreas fault, they will increase the magnitude and spatial extent of time-dependent deformation in that direction [Kenner and Segall, 1999a]. The postseismic redistribution of stress will be governed by the spatial distribution of these low viscosity structures. As earthquake-induced stress gradients in the seismogenic crust are reduced, surface velocities to the northeast of the San Andreas fault will be increased [Kenner and Segall, 1999a]. This results in a deformation field that is asymmetric with respect to the San Andreas fault. Finally, if the San Andreas and Hayward-Rogers Creek-Maacama faults dip toward one another, as proposed by Parsons and Hart [1998], this will produce asymmetries that could also help to explain the observed distribution of deformation though time. Preliminary modeling indicates that faults with this geometry will concentrate postseismic deformation between them. At certain locations this can increase fault parallel strain accumulation rates [Kenner and Segall, 1999b]. In all probability, some combination of these mechanisms will be required to explain the asymmetry in the data through time.

Although our velocity estimates depend on a prior model to constrain rigid body translations, rotation, and scale, when they are combined with estimates of shear strain rate, we have better spatial resolution than previous results. In addition, these represent the only currently available velocity estimates for post-1906 deformation. Further, while the inversions do not provide well-constrained bounds on the depth distribution of slip (Plate 1), they do show how slip velocity varies with time (Figure 6). At both Point Arena and the Point Reyes-Petaluma arc, deformation rates decrease through time following the 1906 earthquake. This means that additional sources of deformation, beyond the simple secular model, are required to explain data from early in the earthquake cycle and that strain accumulation rates are temporally variable. In other words, geodetic measurements made many decades after a great event are not representative of the much higher loading rates immediately following a great earthquake.

5. Conclusions

In summary, we have used the methods of Yu and Segall [1996] to reanalyze historical triangulation data following the 1906 San Francisco earthquake. As this event provides one of the only sources of information regarding deformation following great earthquakes within the San Andreas fault system, any additional information, even if the uncertainties are large compared to more modern geodetic measurements, is extremely valuable in constraining existing models of postseismic deformation and lower crustal structure and rheology. This analysis has greatly increased both the temporal and spatial resolution of the applicable data in northern California.

The approach is most useful in the analysis of networks with short baselines such as the Point Arena and Point Reyes-Petaluma networks. Because the uncertainties grow with baseline length, networks with long baselines, such as the northern California primary network, did not generate reasonable velocity estimates. Unfortunately, this meant that efforts to obtain a postseismic velocity estimate for the Farallon Islands, 40 km to the southwest of the San Andreas fault, have been inconclusive.

With the addition of more recent geodetic results, we have been able to infer an effective exponential relaxation time for long-term postseismic deformation following the 1906 earthquake of $36 \pm 16$ years. This result agrees with the 30-year estimate of Thatcher [1983] using uniform shear strain rate data from the entire San Andreas fault system. Additionally, and for the first time, we have been able to make estimates of the post-1906 station velocities. Therefore we now have velocity profiles corresponding to each of the strain rate data points used in the estimates of relaxation time at Point Arena and Point Reyes.

The availability of localized shear strain rate measurements and individual station velocity estimates allows us to consider local variations in the spatial distribution of postseismic deformation following the 1906 San Francisco earthquake. Inferences concerning the appropriate models required to fit these data are mixed. Because of a lack of spatial resolution, particularly at Point Arena, inversions for the best fitting models are not well constrained, though, when taken in total, they do permit some conclusions. At both Point Arena and the Point Reyes-Petaluma the rate of deformation, on whatever structures are controlling the deformation, must change with time. At Point Arena the data can be satisfactorily fit with accelerated afterslip at depth along the San Andreas fault plane. For a 10-km-deep, 25-km-wide afterslip zone the average slip rate between 1906 and 1930 is 11.2 cm/yr. Between 1929 and 1975 it is 4.6 cm/yr. Inversions of the Point Arena data indicate that the width of the afterslip zone is unconstrained. If the characteristic coseismic slip is assumed to be $< 5.5 \text{ m}$, then the top of the zone of accelerated afterslip must be shallower than 20 km. Data from the Point Reyes-Petaluma arc clearly show
asymmetric deformation with respect to the trace of the San Andreas fault, especially between 1929 and 1939. A closer look at geologically reasonable geometries, with slip rates determined from the inversion results, reveals that accelerated deep afterslip models do not explain particularly well the breadth of the deformation field to the northeast of the San Andreas fault, especially between 1929 and 1939. Both accelerated deep afterslip and horizontal detachment models have trouble explaining spatial variations in the deformation field through time. In other words, no single fault geometry can satisfactorily explain both the 1929-1939 and 1938-1961 data. As a result, some more complex mechanism, or combination of mechanisms, is needed to describe the Point Keyes-Petuluma arc results.

Acknowledgments. We thank Richard Syui for compiling the original dataset obtained from NGS, Mark Murray for his advice and help in analyzing the GPS data, and Roland Bürgmann for the use of his secular deformation model. Reviews by Wayne Thatcher, Roland Bürgmann, Stephanie Prejean, the Associate Editor, and an anonymous reviewer improved the manuscript. This work was supported by USGS grant 1434-HQ-97-GR-03122 and NSF grant EAR-9526910 to Stanford University.

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(Received June 28, 1999; revised January 31, 2000; accepted March 2, 2000)